

ON RECURRENT LIGHTLIKE HYPERSURFACE OF KENMOTSU MANIFOLD

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(Received: Aug. 30, 2021 Accepted: Nov. 28, 2022 Published: Dec. 30, 2022)

Abstract: The object of present paper is to study the properties of recurrent lightlike hypersurfaces of Kenmotsu manifold with (ℓ, m) -type connection.

Keywords and Phrases: Hypersurfaces, Kenmotsu manifold, Recurrent lightlike hypersurfaces.

2020 Mathematics Subject Classification: 53C15, 53C25.

1. Introduction

A linear connection $\bar{\nabla}$ on a semi-Riemannian manifold (\bar{M}, \bar{g}) is called an (ℓ, m) -type connection [7] if $\bar{\nabla}$ and its torsion tensor \bar{T} satisfy

$$\begin{aligned}(\bar{\nabla}_{\bar{X}}\bar{g})(\bar{Y}, \bar{Z}) &= \ell\{\theta(\bar{Y})\bar{g}(\bar{X}, \bar{Z}) + \theta(\bar{Z})\bar{g}(\bar{X}, \bar{Y}) \\ &\quad - m\{\theta(\bar{Y})\bar{g}(J\bar{X}, \bar{Z}) + \theta(\bar{Z})\bar{g}(J\bar{X}, \bar{Y})\}\end{aligned}\tag{1.1}$$

and

$$\bar{T}(\bar{X}, \bar{Y}) = \ell\{\theta(\bar{Y})\bar{X} - \theta(\bar{X})\bar{Y}\} + m\{\theta(\bar{Y})J\bar{X} - \theta(\bar{X})J\bar{Y}\},\tag{1.2}$$

where ℓ and m are two smooth functions on \bar{M} , J is a tensor field of type $(1, 1)$ and θ is a 1-form associated with a smooth unit vector field ζ which is called the characteristic vector field of \bar{M} , given by $\theta(\bar{X}) = \bar{g}(\bar{X}, \zeta)$. By direct calculation it